

**Pro-One**

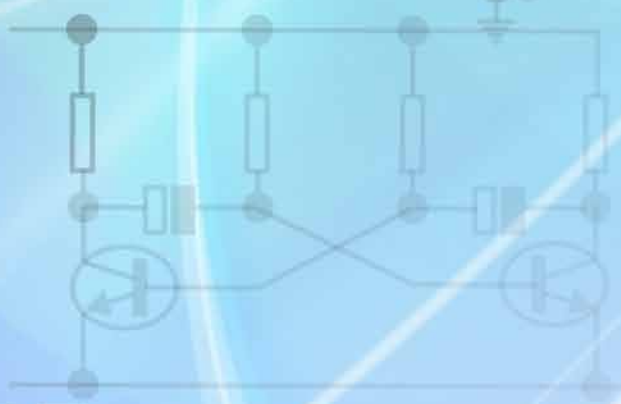


**GATE**

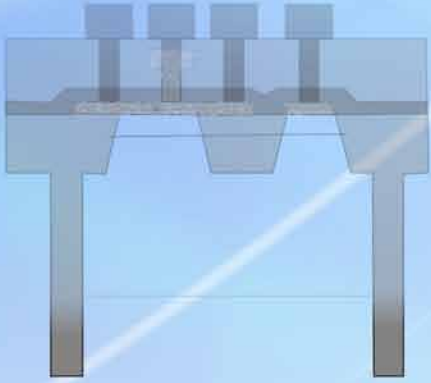


**Graduate Aptitude Test in Engineering**

**Electronics and Communication Engineering**



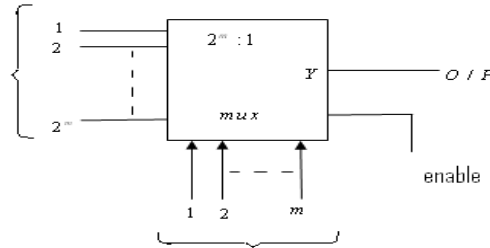
**Sample Booklet**



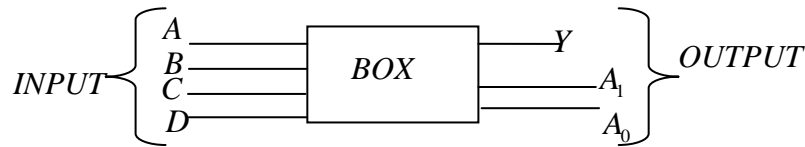
**btechguru.com**

## DIGITAL CIRCUITS

- **MULTIPLEXER** → multiplexer take  $2^m$  inputs, 'm' select lines and having one output transparency of inputs to the output depend on select line.



1. Consider we have four p line i/p and one o/p line as below



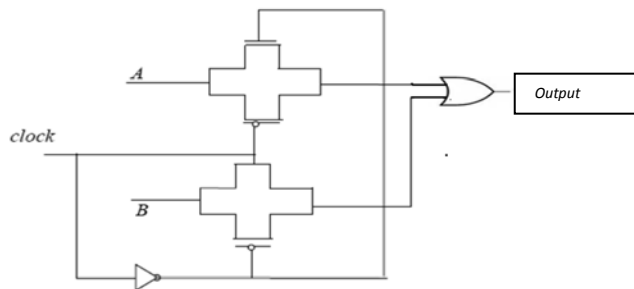
If we want to select i/p depends on address line generated by control unit, which element is best suited for box?

- a. Decoder      b. Demux      c. ALU      d. MUX

**Answer: (d)**

**Solution:** if one have multiple i/p M and have o/p '1' with select lines x then, MUX is useful element and it hold following relation  $2^x=N$

2. Consider a circuit shown below.



Where A, B=input, and O/P is taken at the output of OR gate present at the right most

Part which logic block it represent?

- a. Demux   b. MUX   c. multiplexer   d. encoder

**Answer: b**

**Solution:**

Circuit shown in above problem have i/p A and B, it produce o/p depend upon clock logic level, thus clock act as select line. Hence final equivalent block will be as above.

---

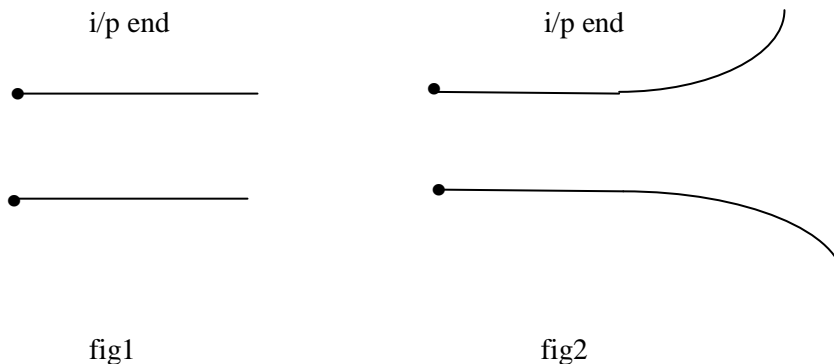
## ELECTROMAGNETICS

**Antenna:**

If the physical dimensions of current carrying element are comparable to the wavelength then it acts as a radiator (antenna).

In fact current carrying conductors radiate energy at all frequencies, but the radiation will be significant only when above condition is satisfied.

For example transmission line in Fig-2 has more radiation then that in fig1.



While in fig1, the amount of propagation is more than the amount of radiation when compared with fig2.

**Antenna gain:**

Any point in space can be represented using a 3 dimensional co-ordinate system such as, Cartesian (with x-axis, y-axis and z-axis) or Spherical or Cylindrical co-ordinate systems. Each of these are orthogonal systems.

## QUESTIONS

**1.The length of a half wave dipole antenna to be used to receive a 10Mhz radio**

**signal=\_\_\_\_\_**

- a.15m                      b.30m                      c.300m                      d.3km**

**Answer: (a)**

**Solution:**

$$f = \frac{c}{\lambda} \Rightarrow \lambda = \frac{3 \times 10^8}{10^7} = 30m \quad \text{Length of half wave dipole antenna} = \frac{\lambda}{2} = 15m$$

---

**2. A short vertical grounded antenna is designed to radiate at**

**1 MHz will have a radiation resistance of \_\_\_\_\_  $\Omega$ , if the effective**

**Length of the antenna is  $\frac{30}{\pi}m$**

- (a) 1.6            (b) 3.2            (c) 15.8            (d) none

**Answer :(a)**

**Solution:**

$$\text{Radiation resistance} = \frac{160\pi^2 l_e^2}{\lambda^2} \Omega = \frac{160\pi^2 \left(\frac{30}{\pi}\right)^2}{300 \times 300} \Omega = 1.6\Omega$$

---

### SIGNALS AND SYSTEMS

A signal by definition anything that conveys some information.

**Periodic signal:**

A signal  $f(t)$  is said to be periodic with period( a non zero real number ) if

$$F(t+T)=f(t) \text{ and } T \text{ is the minimum}$$

**1. Period of the function  $\sin\left(\frac{\pi}{26}(t-1950)\right)$  is \_\_\_\_\_ in seconds**

- (a) 26            (b) 1950            (c)  $\frac{\pi}{13}$             (d) 52

**Answer: (d)**

**Solution:**

$$\sin\left(\frac{\pi}{26}(t-1950)\right) = \sin\left(\frac{2\pi t}{52} - \frac{\pi(1950)}{26}\right)$$

Comparing with  $\sin\left(\frac{2\pi t}{T} + \phi\right) = 52 \text{ sec}$

---

**Convolution in time domain:**

$$\begin{aligned} \text{If } f(t) &\stackrel{L}{\leftrightarrow} F(s), g(t) \stackrel{L}{\leftrightarrow} G(s), \text{ then} \\ L\{f(t) * g(t)\} &= F(s)G(s) \end{aligned}$$

Where  $f(t)*g(t)$  is the convolution of  $f(t)$  and  $g(t) = \int_0^t f(v)g(t-v)dv$

**Example:**

1. To find inverse Laplace transform of  $\frac{1}{s(s+1)}$  using convolution theorem

$$\text{Sol: } L^{-1}\left[\frac{1}{s(s+1)}\right] = L^{-1}\left[\frac{1}{s} - \frac{1}{s+1}\right]$$

Let  $F(s)=1/s \Rightarrow f(t)=u(t)$

$$G(s) = \frac{1}{s(s+1)} \Rightarrow g(t) = e^{-t}u(t)$$

Where  $u(t)$  is unit step function,  $u(t) = \begin{cases} 1, t \geq 0 \\ 0, t < 0 \end{cases}$

2.  $\delta(-t+1) * \delta(t-8) =$

(a)  $\delta(9)$       (b)  $\delta(t-9)$       (c)  $\delta(2t-9)$       (d)  $\delta(t+9)$

**Answer: (d)**

3. Odd part of the function  $\alpha(t) = \delta(t) + u(t)$  is

(a)  $\frac{u(t) - u(-t)}{2}$       (b)  $\delta(t) + u(t)$       (c) 0      (d)  $\frac{\delta(t)}{2} + \frac{u(t)}{2} + \frac{\delta(-t)}{2} + \frac{u(-t)}{2}$

**Answer :(a)**

**Solution:**

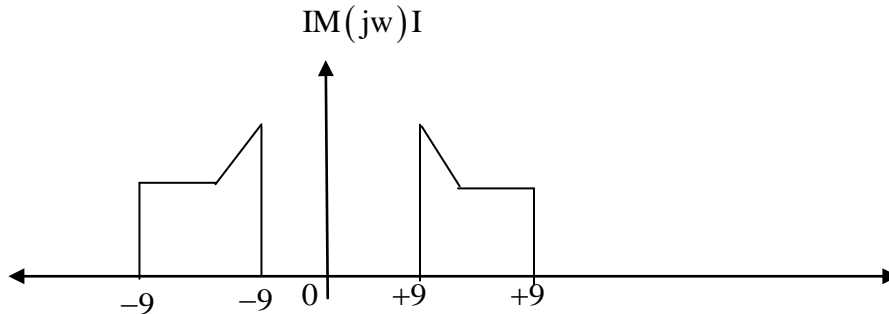
Odd part of a signal  $\alpha(t)$  is given by  $\frac{\alpha(t) - \alpha(-t)}{2}$

Further  $\delta(t) = \delta(-t)$  [Impulse function is an even function]

---

**Sampling theorem:**

1. The spectral range of a signal  $m(t)$  extend from 9khz to 9.9khz as shown in fig.



The minimum sampling frequency needed for recovery of the signal =

- (a) 19.8khz      (b) 1.8khz      (c) 18khz      (d) 18.9khz

**Answer:(c)**

**Solution:**

For band pass kind of signals min. samples frequency =  $f_{min} = 2(F_{max} - F_{min})$

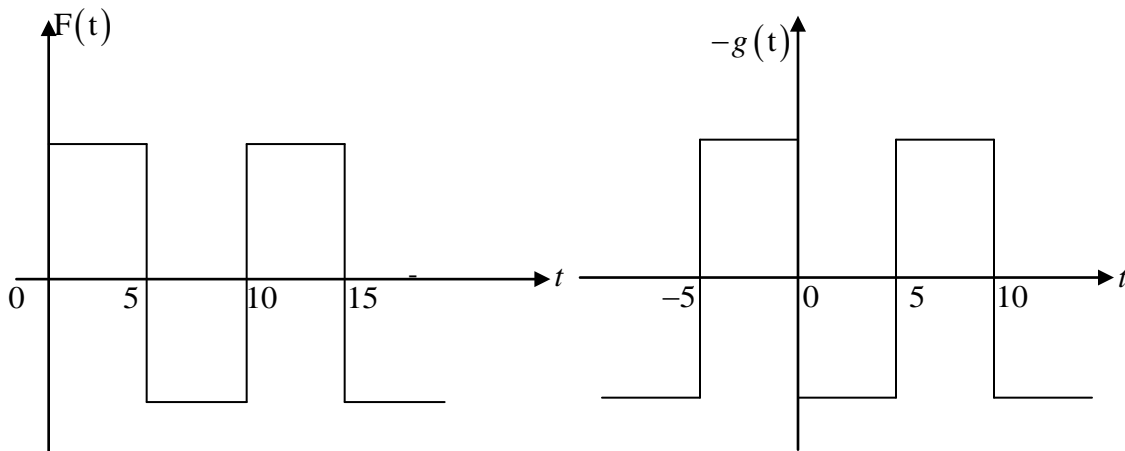
If at least one of  $f_{max}$  or  $f_{min}$

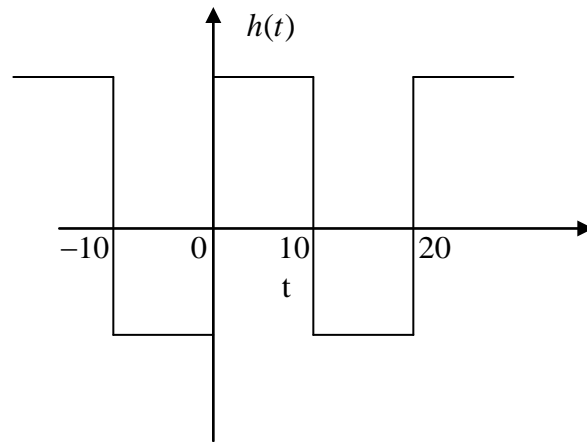
Here  $f_{max}=9.9\text{khz}$ ,  $F_{min}=9\text{khz}$

$f_{min}=1.8\text{khz}$  is called because  $f_{min}/f_{max}=5=\text{an integer}$

Note: Please see next question also. For band pass signals sampling frequency formula is not always same as that for low pass signals for which  $f_{min}=0\text{hz}$

2: Two signals  $f(t)$   $g(t)$  are  $h(t)$  are as shown in fig. which signal needs higher sampling frequency if the samples?





- (a)  $f(t)$  and  $h(t)$       (b)  $g(t)$  and  $h(t)$       (c)  $f(t)$  and  $g(t)$       (d)  $h(t)$

**Answer: (c)**

**Solution:**

$f(t)$  and  $g(t)$  have same time period and its is half of that of  $h(t)$ . so frequency content of  $f(t)$  and  $g(t)$  will be higher than that of  $h(t)$ .

---

**3: If message signals having highest frequency component of 9khz needs to be processed and be transmitted as pulse coded modulated then the bit rate will be \_\_\_ if PCM is supposed to have 128 levels and if the original signal has to be reconstructed in the receiver with minimum distortion.**

- (a) 7 Bits      (b) 8 Bits      (c) 6 Bits      (d) 5 Bits

**Answer: (a)**

**Solution:**

Highest frequency component in the modulating message signal = 9khz =  $f_{max}$

$\Rightarrow$  Minimum sampling frequency = 18KHZ (=  $2f_{max}$ )

i.e, 18000 sample/second

128 levels  $\Rightarrow$  7bits ( $\because 2^7 = 128$ )